edexcel

January 2007 6683 Statistics S1 Mark Scheme

Question number	Scheme	Marks	
1. (a)	(£) 17 Just <u>17</u>	B1	(1)
(b)	$\sum t = 212$ and $\sum m = 61$ (Accept as totals under each column in qu.)	B1, B1	
	$S_{tm} = 2485 - \frac{61 \times 212}{10}$, = 1191.8 awrt <u>1190</u> or 119 (3sf)	M1, A1	
	$S_{tt} = 983.6 \text{ (awrt 984)} \text{ and } S_{mm} = 1728.9 \text{ (awrt 1730)} \text{ (or 98.4 and 173)}$	A1, A1	(6)
(c)	$r = \frac{1191.8}{\sqrt{983.6 \times 1728.9}}$	M1, A1f.t.	
	= 0.913922 awrt <u>0.914</u>	A1	(3)
(d)	0.914 (Must be the same as (c) or awrt 0.914)	B1f.t. (<i>r</i> <1)
	e.g. linear transformation, coding does not affect coefficient (or recalculate)	dB1	(2)
(e)	0.914 suggests longer spent shopping the more spent. (Idea more time, more spent) B1	
	0.178 different amounts spent for same time.	B1	(2)
(f)	e.g. might spend short time buying 1 expensive item <u>OR</u> might spend a long time		
	checking for bargains, talking, buying lots of cheap items.	B1g	(1)
		15 ma	ırks
(b)	M1 for one correct formula seen, f.t. their $\sum t$, $\sum m$ [Use 1 st A1 for 1 correct, $\sum t$]	2^{nd} A1 for 2 et	tc]
(c)	M1 for attempt at correct formula, $\frac{2485}{\sqrt{2101 \times 5478}}$ scores M1A0A0		
	A1ft f.t. their values for S_{tt} etc from (b) but don't give for $S_{tt} = 5478$ etc (see ab	oove)	
	Answer only (awrt 0.914) scores 3/3, 0.913 (i.e. truncation) can score M1A1ft by i	mplication.	
(d)	2 nd B1 dependent on 1 st B1 Accept $\sum m = 261, \sum m^2 = 8541, \sum tm = 6725 \rightarrow 0.9$	014	
(e)	One mark for a sensible comment relating to each coefficient		
	For 0.178 allow "little or no link between time and amount spent". Must be in con	itext.	
	Just saying 0.914 is strong +ve correlation between amount spent and time shopping	ng and	
	0.178 is weak correlation scores B0B0.		
(f)	B1g for a sensible, practical suggestion showing that other factors might affect t	the amount sp	ent.
	E.g. different day (weekend vs weekday) or time of day (time spent queuing if bus	y)	
1			

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2. (a)	$\begin{array}{c} 0.03 D (0.0105) \\ \hline A \\ \hline \end{array} \qquad \qquad$	M1
	0.35 \overline{D} \overline{D} $A, B \text{ and } C \text{ and } 0.35 \text{ and } 0.25$ 0.06 D (0.015) $A, B \text{ and } C \text{ and } 0.35 \text{ and } 0.25$	A1
	0.25 B $D(x3) and 0.03, 0.06, 0.05$	A1 (3)
	\overline{D} (May be implied by seeing	
	0.05 D (0.02) $P(A \cap D)$ etc at the ends)	
	\sim_{C}	
	\overline{D}	
(b)(i)	$P(A \cap D) = 0.35 \times 0.03$, $= 0.0105$ or $\frac{21}{2000}$	M1, A1
	P(C) = 0.4 (anywhere)	B1
(ii)	$P(D) = (i) + 0.25x \ 0.06 + (0.4x \ 0.05)$	M1
	$=$ <u>0.0455</u> or $\frac{91}{2000}$	A1 (5)
(c)	$P(C D) = \frac{P(C \cap D)}{P(D)}, = \frac{0.4 \times 0.05}{(ii)}$	M1, A1ft
	= 0.43956 or $\frac{40}{91}$ <u>0.44</u> or awrt <u>0.440</u>	A1 (3)
	[Correct answers only score full marks in each part]	11 marks
(a)	M1 for tree diagram, 3 branches and then two from each. At least one probability	ity attempted.
(b)	1 st M1 for 0.35x0.03. Allow for equivalent from <u>their tree diagram.</u>	
	B1 for $P(C) = 0.4$, can be in correct place on tree diagram or implied by 0.4×0.4	
	2^{nd} M1 for all 3 cases attempted and <u>some</u> correct probabilities seen, including +. (
	Condone poor use of notation if correct calculations seen. E.g. $P(C D)$ for	$P(C \cap D)$.
(c)	M1 for attempting correct ratio of probabilities. There must be an attempt to su	
	values in a correct formula. If no correct formula and ration not correct ft s	core M0.
	Writing $P(D C)$ and attempting to find this is M0.	
	Writing $P(D C)$ but calculating correct ratio – ignore notation and mark ratio	OS.
	A1ft must have their 0.4×0.05 divided by their (ii).	
	If ratio is incorrect ft $(0/3)$ unless correct formula seen and part of ratio is co	orrect then M1.

Question Number	Scheme	Marks	
3. (a)	N.B. Part (a) doesn't have to be in a table, could be a list $P(X=1) = \dots$ etc	B1, B1, B1	
	x 1 2 3 4 5 6		
	$P(X=x) \frac{1}{36} \frac{3}{36} \frac{5}{36} \frac{7}{36} \frac{9}{36} \frac{11}{36}$		
	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	(3)	
(b)	$P(3) + P(4) + P(5) = \frac{21}{21} \text{ or } \frac{7}{21} \text{ or a wrt } 0.583$	M1, A1 (2)	
	$P(3) + P(4) + P(5) =, \frac{21}{36} \text{ or } \frac{7}{12} \text{ or awrt } 0.583$	M1, A1 (2)	
(c)	$E(X) = \frac{1}{36} + 2 \times \frac{3}{36} + \dots, = \frac{161}{36} \text{ or } 4.472 \text{ or } 4\frac{17}{36}$	M1, A1 (2)	
(d)	$E(X^2) = \frac{1}{36} + 2^2 \times \frac{3}{36} + \dots, = \frac{791}{36}$ or full expression or $21\frac{35}{36}$ or awrt 21.97	M1, A1	
	$\operatorname{Var}(X) = \frac{791}{36} - \left(\frac{161}{36}\right)^2$, $= \underline{1.9714*}$	M1, A1c.s.o. (4)	
(e)	$Var(2-3X) = 9 \times 1.97$ or $(-3)^2 \times 1.97$, = 17.73 awrt <u>17.7</u> or $\frac{2555}{144}$	M1, A1 (2)	
		13 marks	
(a)	1 st B1 for $x = 1,, 6$ and at least one correct probability N.B. $\frac{3}{36} = \frac{1}{12}$ and $\frac{9}{36} = \frac{1}{4}$	-	
	2 nd B1 for at least 3 correct probabilities		
	3 rd B1 for a fully correct probability distribution.		
(b)	M1 for attempt to add the correct three probabilities, ft their probability distribution	ution	
(c)	M1 for a correct attempt at $E(X)$. Minimum is as printed. Exact answer only s	cores M1A1.	
	[Division by 6 at any point scores M0, no ISW. Non-exact answers with no worki	ng score M0.]	
(d)	1 st M1 for a correct attempt at $E(X^2)$. Minimum as printed. $\frac{791}{36}$ or awrt 21.97 scores M1A1.		
	2^{nd} M1 for their E(X ²) - (their E(X)) ² .		
	2^{nd} A1 cso needs awrt 1.97 and $\frac{791}{36} - \left(\frac{161}{36}\right)^2$ or $\frac{2555}{1296}$ or any fully correct express	ssion seen.	
	Can accept <u>at least 4 sf</u> for both. i.e. 21.97 for $\frac{791}{36}$, 4.472 for $\frac{161}{36}$, 20.00 for $\left(\frac{10}{36}\right)$	$\left(\frac{61}{6}\right)^2$.	
(e)	M1 for correct use of $Var(aX + b)$ formula or a <u>full</u> method.		
	NB $-3^2 \times 1.97$ followed by awrt 17.7 scores M1A1 <u>BUT</u> $-3^2 \times 1.97$ alone, or f	followed by	
	– 17.7, scores M0A0.		

Question Number	Scheme	Marks
4. (a)	Positive skew (both bits)	B1 (1)
(b)	$19.5 + \frac{(60-29)}{43} \times 10, = 26.7093$ awrt <u>26.7</u>	M1, A1 (2)
	(N.B. Use of 60.5 gives 26.825 so allow awrt 26.8)	
(c)	$\mu = \frac{3550}{120} = 29.5833$ or $29\frac{7}{12}$ awrt <u>29.6</u>	B1
	$\sigma^2 = \frac{138020}{120} - \mu^2$ or $\sigma = \sqrt{\frac{138020}{120} - \mu^2}$	M1
	$\sigma = 16.5829$ or (s = 16.652) awrt <u>16.6</u> (or s = 16.7)	A1 (3)
(d)	$\frac{3(29.6 - 26.7)}{16.6}$	M1A1ft
	= 0.52	A1 (3)
(e)	0.520 > 0correct statement about their (d) being >0 or < 0	B1ft dB1ft (2)
(f)	Use <u>Median</u> Since the data is skewed <u>or</u> less affected by outliers/extreme values	B1 dB1 (2)
(g)	If the data are <u>symmetrical</u> or <u>skewness is zero</u> or <u>normal/uniform distribution</u> ("mean =median" or "no outliers" or "evenly distributed" all score B0)	B1 (1) 14 marks
(b)	M1 for (19.5 or 20) + $\frac{(60-29)}{43}$ ×10 or better. Allow 60.5 giving awrt 26.8 for	M1A1
	Allow their $0.5n$ [or $0.5(n+1)$] instead of 60 [or 60.5] for M1.	
(c)	M1 for a correct expression for σ , σ^2 , s or s^2 . NB $\sigma^2 = 274.99$ and $s^2 = 277.30$ Condone poor notation if answer is awrt16.6 (or 16.7 for s))
(d)	 M1 for attempt to use this formula using their values to any accuracy. Condone 1st A1ft for using their values to at least 3sf. Must have the 3. 2nd A1 for using accurate enough values to get awrt 0.520 (or 0.518 if using s) NB Using only 3 sf gives 0.524 and scores M1A1A0 	e missing 3.
(e)	1^{st} B1 for saying or implying correct sign for their (d). B1g and B1ft. Ignore "co 2^{nd} B1 for a comment about consistency with their (d) and (a) being positive skew This is dependent on 1^{st} B1: so if (d)>0, they say yes, if (d)<0 they say no.	
(f)	2 nd B1 is dependent upon choosing median.	

Question Number	Scheme	Mark	(S
5. (a)	Time is a <u>continuous</u> variable <u>or</u> data is in a <u>grouped</u> frequency table	B1	(1)
(b)	Area is proportional to frequency or $A \propto f$ or $A = kf$	B1	(1)
(c)	$3.6 \times 2 = 0.8 \times 9$ 1 child represented by 0.8	M1 dM1 A1 cso	(3)
(d)	$(\text{Total}) = \frac{24}{0.8}, = \underline{30}$	M1, A1 7 m	(2) arks
(b)	1 st B1 for one of these correct statements. "Area proportional to frequency density" or "Area = frequency" is B0	1	
(c)	1 st M1 for a correct combination of any 2 of the 4 numbers: 3.6, 2, 0.8 and 9 e.g. 3.6×2 or $\frac{3.6}{0.8}$ or $\frac{0.8}{2}$ etc BUT e.g. $\frac{3.6}{2}$ is M0 2 nd M1 dependent on 1 st M1 and for a correct combination of 3 numbers leading to May be in separate stages but must see all 4 numbers A1cso for fully correct solution. Both Ms scored, no false working seen and <u>com</u>		<u>ed.</u>
(d)	M1 for $\frac{24}{0.8}$ seen or implied.		

Scheme	Marks	
Used to simplify <u>or</u> represent a real world problem Cheaper <u>or</u> quicker <u>or</u> easier (than the real situation) <u>or</u> more easily modified To improve understanding of the real world problem Used to predict outcomes from a real world problem (idea of predictions)	(any two lines) B1 B1 () (2)
(3 or 4) Model used to make predictions. (Idea of predicted values based on the model)	B1	
(4 or 3) (Experimental) data collected	B1	
(7) Model is refined.	B1 (5 marl	(3) ks
 1st B1 For one line 2nd B1 For a second line Be generous for 1st B1 but stricter for B1B1 		
 1st & 2nd B1 These two points can be interchanged. Idea of values from (experimental) data and predicted values based on the model. 1st B1 for predicted values from model e.g. "model used to gain suitable data" 2nd B1 for data collected. Idea of experimental data but "experiment" needn't be explicitly seen 3rd B1 This should be stage 7. Idea of refinement or revision or adjustment 		
	Used to simplify <u>or</u> represent a real world problem Cheaper <u>or</u> quicker <u>or</u> easier (than the real situation) <u>or</u> more easily modified To improve understanding of the real world problem Used to predict outcomes from a real world problem (idea of predictions) (3 or 4) Model used to make predictions. (Idea of predicted values based on the model) (4 or 3) (Experimental) data collected (7) Model is refined. 1 st B1 For one line 2 nd B1 For a second line Be generous for 1 st B1 but stricter for B1B1 1 st & 2 nd B1 These two points can be interchanged. Idea of values from (experimental) data and predicted values based 1 st B1 for predicted values from model e.g. "model used to gain suitable data" 2 nd B1 for data collected. Idea of experimental data but "experiment" needn't be of	Used to simplify <u>or</u> represent a real world problem Cheaper <u>or</u> quicker <u>or</u> easier (than the real situation) <u>or</u> more easily modified To improve understanding of the real world problem Used to predict outcomes from a real world problem (idea of predictions) (3 or 4) Model used to make predictions. (Idea of predicted values based on the model) (4 or 3) (Experimental) data collected (7) Model is refined. 1 st B1 For one line 2 nd B1 For a second line Be generous for 1 st B1 but stricter for B1B1 1 st & 2 nd B1 These two points can be interchanged. Idea of values from (experimental) data and predicted values based on the model. 1 st B1 for predicted values from model e.g. "model used to gain suitable data" 2 nd B1 for data collected. Idea of experimental data but "experiment" needn't be explicitly seen

Question Number	Scheme	Marks
7. (a)	$P(X < 91) = P(Z < \frac{91 - 100}{15})$ Attempt standardisation	M1
	= P(Z < -0.6)	A1
	= 1 - 0.7257	M1
	= 0.2743 awrt <u>0.274</u>	A1 (4)
(b)	1 - 0.2090 = 0.7910 0.791	B1
	P(X > 100+k) = 0.2090 or $P(X < 100+k) = 0.7910$ (May be implied)	M1
	Use of tables to get $z = 0.81$	B1
	$\frac{100 + k - 100}{15}$,=0.81 (ft their z = 0.81, but must be z not prob.)	M1, A1ft
	k = 12	A1 cao (6)
		10 marks
(a)	1 st M1 for attempting standardisation. $\pm \frac{(91 - \mu)}{\sigma \text{ or } \sigma^2}$. Can use of 109 instead of 91.Us 1 st A1 for -0.6 (or + 0.6 if using 109) 2 nd M1 for 1 – probability from tables. Probability should be > 0.5)	e of 90.5 etc is M0
(b)	1 st B1 for 0.791 seen or implied.	
	1^{st} M1 for a correct probability statement, but must use X or Z correctly. Shown of	on diagram is OK
	2 nd B1 for awrt 0.81 seen (or implied by correct answer - see below) (Calculator g	ives 0.80989)
	2^{nd} M1 for attempting to standardise e.g. $\frac{100 + k - 100}{15}$ or $\frac{k}{15}$	
	$\frac{X-100}{15}$ scores 2 nd M0 until the 100+ k is substituted to give k, but may imply 1 st M	1 if <i>k</i> = 112.15 seen
	1 st A1ft for correct equation for k (as written or better). Can be implied by $k = 12$	2.15 (or better)
	2^{nd} A1 for $k = 12$ only.	
	Answers only	
	k = 112 or 112.15 or better scores 3/6 (on EPEN give first 3 marks)	
	k = 12.15 or better (calculator gives 12.148438) scores 5/6 (i.e loses last	A1 only)
	k = 12 (no incorrect working seen) scores 6/6	
NB	Using 0.7910 instead of 0.81 gives 11.865 which might be rounded to 12. This sh	nould score no
	more than B1M1B0M1A0A0.	